

Type:						
Heat exchanger:	Tube coil heat exchanger without displacement cylinder					
Flow pattern:						
	Inside coil			Around coil		
Medium	R410A			Water		
Mass flow	m _i	0.03354	kg/s	m _a	0.3	kg/s
Volume flow	V _i	2.226e-4	m³/s	V _a	3.036e-4	m³/s
Inlet pressure (abs.)	p	32.89	bar	p	1	bar
Inlet temperature	ϑ _{e,i}	53.1	°C	ϑ _{e,a}	46.41	°C
Outlet temperature	ϑ _{a,i}	52.9	°C	ϑ _{a,a}	50	°C
Mean temperature	ϑ _{m,i}	53	°C	ϑ _{m,a}	48.21	°C
Heat duty	Q _i	-4.5	kW	Q _a	4.5	kW
Heat loss				Q _{v,a}	0	kW
Fouling resistance	f _i	0	m²·K/W	f _a	0	m²·K/W
Density	ρ _i	872.7	kg/m³	ρ _a	988.1	kg/m³
Specific heat capacity	cp _i	2386	J/(kg·K)	cp _a	4180	J/(kg·K)
Thermal conductivity	λ _i	0.07305	W/(m·K)	λ _a	0.6385	W/(m·K)
Dynamic viscosity	η _i	0.08029	mPa·s	η _a	0.5634	mPa·s
For phase change						
Density vapour	ρ _{Di}	150.7	kg/m³	ρ _{Da}		kg/m³
Heat of evaporation	Δhv	133687	J/kg	Δhv		J/kg
Vapour mass fraction inlet	x _e	1	-	x _e		-
Vapour mass fraction outlet	x _a	0	-	x _a		-

Geometry:

Shell outside diameter	Do	44.6	mm	Shell wall thickness	s	3.25	mm
Shell inside diameter	Di	38.1	mm				
Tube outside diameter	do	6.35	mm	Tube wall thickness	si	0.5	mm
Tube inside diameter	di	5.35	mm				
Coil diameter	DC	30.75	mm	Coil pitch	h	8	mm
Coil-shell distance		0.5	mm	Distance of windings	w	8	mm
Number of tubes in the coil				η _R	1	-	
Tube material					Copper		
Thermal conductivity of tube material	λ	318	W/(m·K)				

Valuation:

	Required		Final		Overdesign	
Total exchanger area	A	0.5293	m²	A,f	0.5	m²
Total coil length	lc	2190	mm	lc,f	2069	mm
Tube length per tube	lt	26.53	m	lt,f	25064	mm
Number of windings	N	273.7	-	N,f	258.6	-
per tube						
Heat transfer coefficient (inside)			α _i	2704	W/(m²·K)	
Heat transfer coefficient (outside)			α _a	10108	W/(m²·K)	
Overall heat transfer coefficient			k	1853	W/(m²·K)	
Logarithmic mean temperature diff. LMTD			Δϑ _{log}	4.588	K	
FN Factor (Correction factor for LMTD)			FN	1	-	
Total fouling resistance			f	0	m²·K/W	

Inside coil				Around coil			
							
Flow velocity		9.903	m/s	Flow velocity		0.5765	m/s
				Reynolds number	Re	10050	-
Mean tube wall temperature	ϑ_{wi}	49.1	°C	Mean tube wall temperature	ϑ_{wa}	49.08	°C
Pressure drop	Δp_i		bar	Pressure drop	Δp_a	0.08051	bar
				Inlet nozzle			
Connection arrangement		axial	-	Nominal width		DN 20	
tangential / radial / axial ?				Outside diameter		26.9	mm
				Inside diameter		22.3	mm
				Velocity		0.7774	m/s
				Outlet nozzle			
				Nominal width		DN 20	
				Outside diameter		26.9	mm
				Inside diameter		22.3	mm
				Velocity		0.7774	m/s

Equations

Heat balance:

Inside coil

$$Q_i = m_i \cdot c_{p,i} \cdot (\vartheta_{a,i} - \vartheta_{e,i}) + m_i \cdot (x_e - x_a) \cdot \Delta h_{v,i} =$$

$$0.03354 \text{ kg/s} \cdot 2386 \text{ J/(kg}\cdot\text{K)} \cdot (\vartheta_{a,i} - \vartheta_{e,i}) + 0.03354 \text{ kg/s} \cdot (1-0) \cdot 133687 \text{ J/kg} = -4500 \text{ W}$$

Heat balance:

Around coil

$$Q_a = m_a \cdot c_{p,a} \cdot (\vartheta_{a,a} - \vartheta_{e,a}) = m_a \cdot 4180 \text{ J/(kg}\cdot\text{K)} \cdot (50^\circ\text{C} - 46.41^\circ\text{C}) = 4500 \text{ W}$$

Heat balance:

$$Q_i = -(Q_a - Q_v) = -(4500 \text{ W} - 0 \text{ W}) = -4500 \text{ W}$$

Overall heat transfer coefficient

k = 1853 W/(m²·K)

$$\frac{1}{k} = \left[\frac{1}{\alpha_i} + f_i \right] \cdot \frac{da}{di} + \frac{da \cdot \ln\left(\frac{da}{di}\right)}{2 \cdot \lambda} + \frac{1}{\alpha_a} + f_a \Leftrightarrow$$

$$\frac{1}{1853 \text{ W/(m}^2\cdot\text{K)}} = \left[\frac{1}{2704 \text{ W/(m}^2\cdot\text{K)}} + 0 \text{ m}^2\cdot\text{K/W} \right] \cdot \frac{0.00635 \text{ m}}{0.00535 \text{ m}} + \frac{0.00635 \text{ m} \cdot \ln\left(\frac{0.00635 \text{ m}}{0.00535 \text{ m}}\right)}{2 \cdot 318 \text{ W/(m}\cdot\text{K)}} + \frac{1}{10108 \text{ W/(m}^2\cdot\text{K)}} + 0 \text{ m}^2\cdot\text{K/W}$$

$$Q = k \cdot A \cdot \Delta\vartheta_{\log} \cdot FN = 1853 \text{ W/(m}^2\cdot\text{K)} \cdot 0.5293 \text{ m}^2 \cdot 4.588 \text{ K} \cdot 1 = -4500 \text{ W}$$